Final Exam Review

These review slides and earlier ones found linked to on BlackBoard

Bring a photo ID card: Rocket Card, Driver's License

Exam Time

TR class Monday December 9 12:30 – 2:30

Held in the regular classroom.

Extra office hours in UHall 3014 Monday 10:00-12:30

Covers:

12.1 Counting Methods

- 12.2 Fundamental Counting Principle
- 12.3 Permutations and Combinations
- 13.1 The Basics of Probability
- 13.2 Complements and Unions of Events
- 13.3 Conditional Probability
- 14.1 Organization and Visualizing of Data

3

5

- 14.2 Measures of Central Tendancy
- 14.3 Measures of Dispersion
- 14.4 The Normal Distribution

Know the basic vocabulary of the sections.

2

The test will be multiple choice.

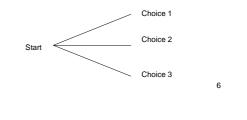
The test will be like the online HW rather than the lab assignments.

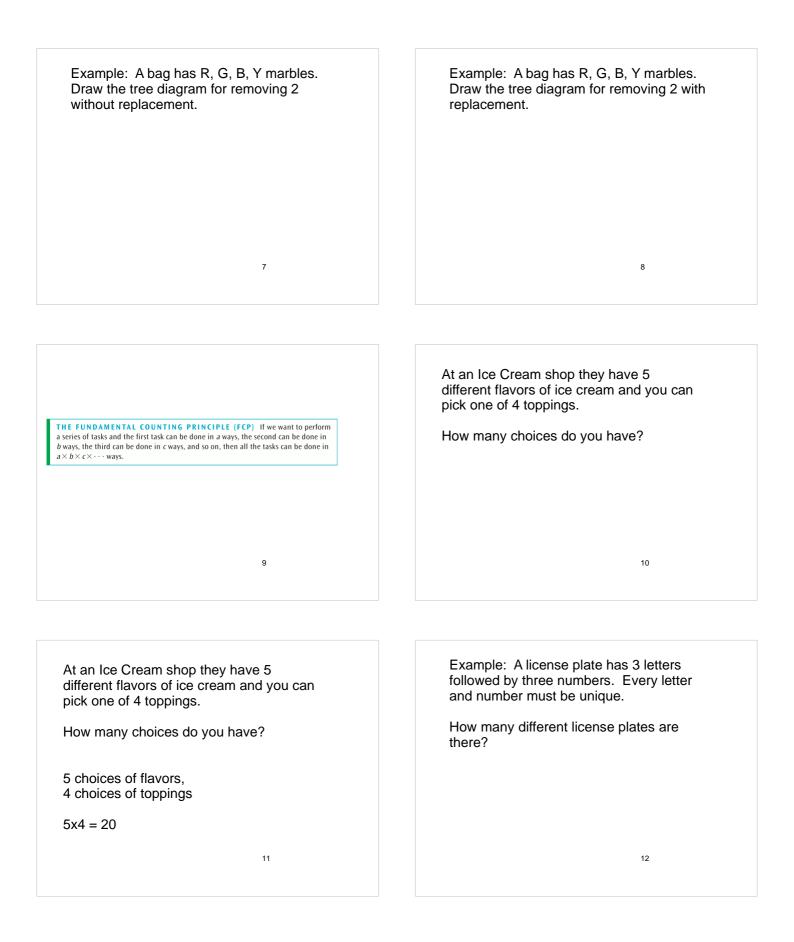
In a selection where repetition is allowed, the phrase **with repetition** is used.

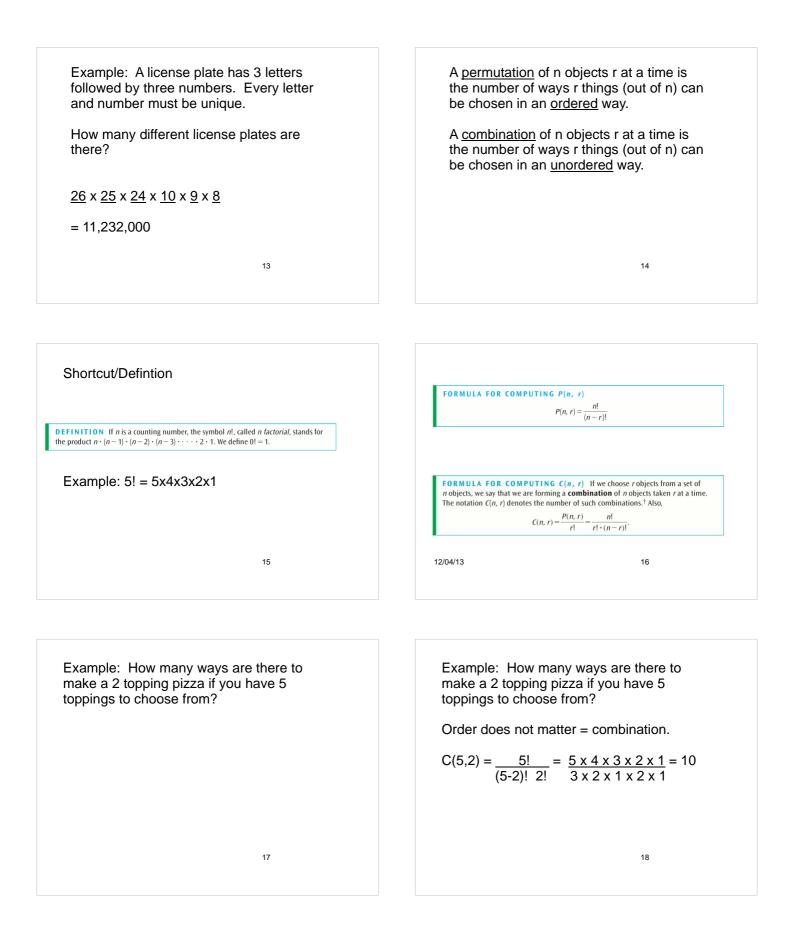
In a selection where repetition is not allowed, the phrase **without repetition** is used.

There is a graphical way to organize and count.

A **tree diagram** is a visual method for each new choice at a step we get a new branch. Work from left to right.







Probability is a fraction (or decimal) An **experiment** is a controlled operation between 0 (doesn't happen) and 1 that yields a set of results. (always happens). The possible results of an experiment are called its outcomes. The set of Probability of Event E = P(E)outcomes are the **sample space**. Theoretical = found mathmatically number of times event happens number of possible outcomes An event is a subcollection of the outcomes of an experiment. Empirical = found by running experiments number of times event happens number of times experiment run 19 20 Example: Experiment is roll a die. Example: Experiment is roll a die. Sample space: { 1, 2, 3, 4, 5, 6 } Sample space: { 1, 2, 3, 4, 5, 6 } What is the probability of rolling an odd What is the probability of rolling an odd number? number? Event $E = \{1, 3, 5\}$ P(E) = 3/6 = 1/221 22

Odds and probability are similar.

Probability #(it happens) / #(total)

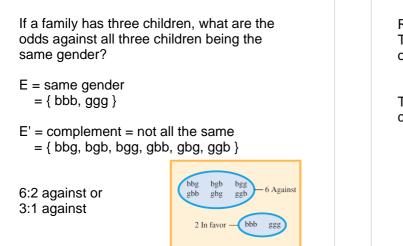
Odds for #(it happens) : #(it does not happen)

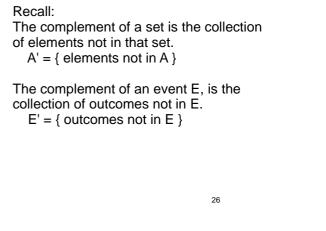
Odds against #(it does not happen) : #(it happens)

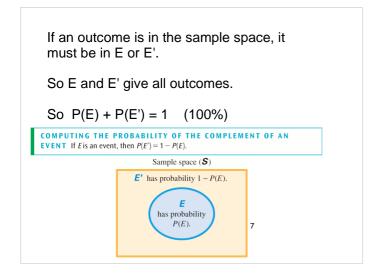
23

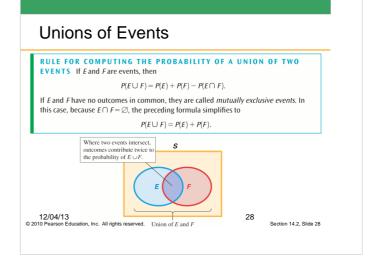
If a family has three children, what are the odds against all three children being the same gender?

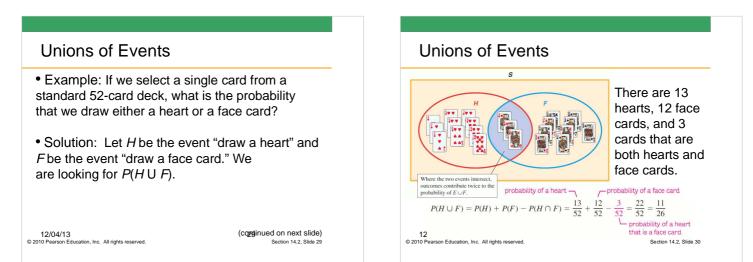
24



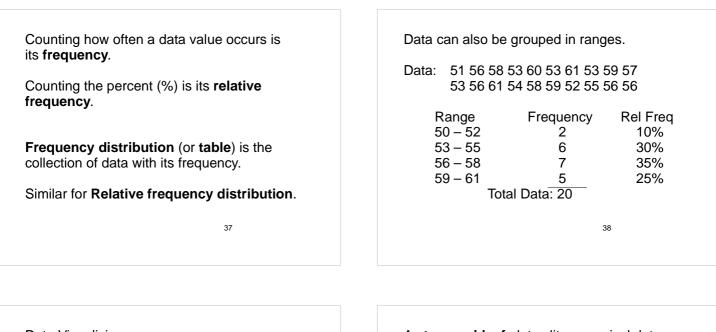


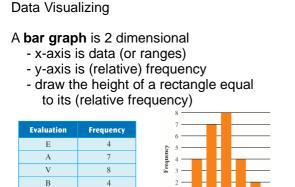






If you are given 3 out of the 4 terms in the equation $P(E \cup F) = P(E) + P(F) - P(E \cap F)$ Then you can use algebra to find the remaining term. This can also be read as P(E or F) = P(E) + P(F) - P(E and F) ³¹	Conditional probability is the probability of one event (F) happening assuming that another event (E) does. Examples: - probability that someone is happy given that they just won \$\$\$. - probability that someone passes an exam given that they did not study. The probability that F happens given that E does is denoted P(F E) It is read "probability of F given E ³⁷
Example: Roll a die for an experiment.	Example: Roll a die for an experiment.
What is the probability it is odd given that the value was a prime number?	What is the probability it is odd given that the value was a prime number? The event assumed to happen was that the value was prime.
	Among those the event is when is it odd.
33	34
Example: Roll a die for an experiment.	The previous examples lead to a way to
What is the probability it is odd given that the value was a prime number?	count P(F E) by a formula:
The event assumed to happen was that the value was prime. { 2, 3, 5 }	SPECIAL RULE FOR COMPUTING $P(F E)$ BY COUNTING If <i>E</i> and <i>F</i> are events in a sample space with equally likely outcomes, then $P(F E) = \frac{n(E \cap F)}{n(E)}$.
Among those the event is when is it odd.	
{ 3, 5 }	



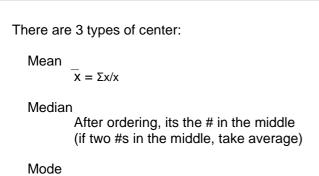


2

25

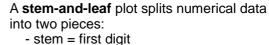
Р

Total



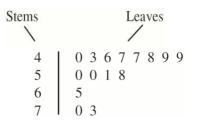
The number which occurs the most (if more than one \rightarrow multimodal) (if none \rightarrow no mode) ₄₁

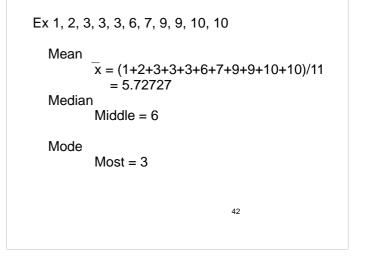
Viewers' Ratings

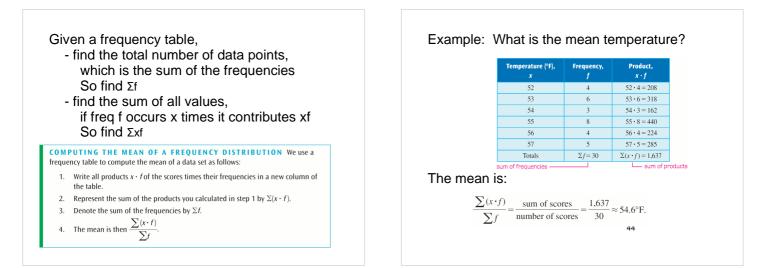


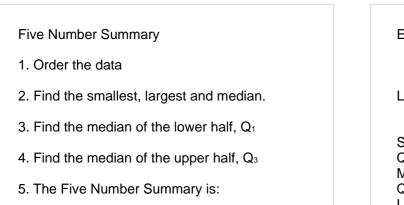
- leaf = last digit

46 43 40 47 49 70 65 50 73 49 47 48 51 58 50

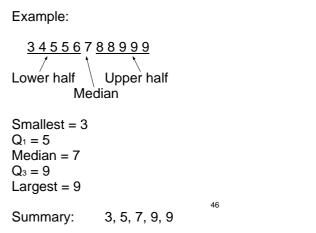


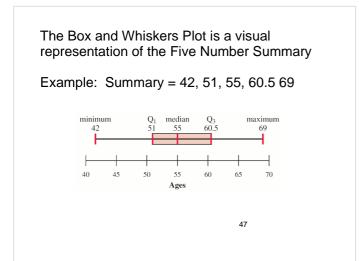




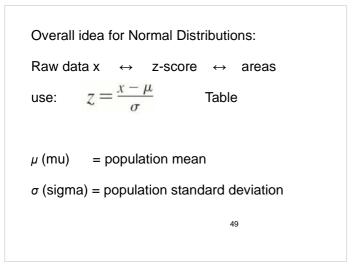


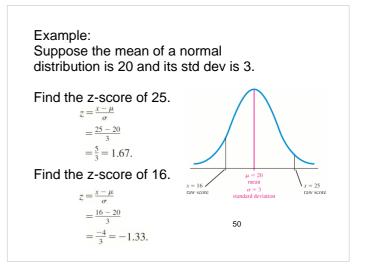
smallest, Q1, median, Q3,4 argest





Definition Std. D		$n = \sqrt{\frac{\Sigma (x - \bar{x})^2}{n - 1}}^2$	
Data x	x- x	$(x-\overline{x})^2$	
2	-3	9	variance
4	-1	1	= 24/5
7	2	4	= 1.2
5	0	0	
4	-1	1	std. dev.
8	3	9	$= (1.2)^{1/2}$
		1	₄₈ = 1.09544
Sum (Σ)	0	24	





The area between z-scores gives the percent of data values between them.

Below is a table that gives the area between the mean (μ) and a given z-score.

0.05 0.02 0.61 2.29 1.17 3.79 1.73 4.58 2.29 4.89 2.85 4.98 0.07 0.28 6.23 2.32 1.18 3.81 1.74 4.59 2.20 4.89 2.85 4.98 0.07 0.28 6.63 2.32 1.18 3.81 1.74 4.59 2.20 4.89 2.85 4.98 0.70 0.28 6.3 2.36 1.19 3.81 1.75 4.60 2.31 4.90 2.87 4.98 0.80 0.32 6.4 2.39 1.20 3.85 1.76 4.60 2.31 4.90 2.87 4.98 0.90 0.36 6.5 2.42 1.21 3.87 1.77 4.62 2.33 4.90 2.89 4.98 0.90 0.66 2.45 1.22 3.89 1.78 4.63 2.34 4.90 2.90 4.98 0.90 0.66 2.45 1	0.1 .004 .57 .216 1.13 .371 1.69 .455 2.25 .488 2.81 .498 0.2 .008 .58 .219 1.14 .373 1.70 .455 2.22 .488 2.82 .498 0.3 .012 .59 .222 1.15 .375 1.71 .455 2.26 .488 2.82 .498 0.4 .016 .60 .226 1.16 .377 1.72 .457 2.28 .489 2.83 .498 0.4 .016 .60 .226 1.16 .377 1.72 .457 .228 .489 2.83 .498 0.05 .020 .61 .229 1.17 .379 1.73 .458 .230 .489 .285 .498 0.06 .024 .62 .232 .118 .381 1.74 .459 .230 .489 .286 .498 0.7 .028 .63							
0.02 0.08 .58 .219 1.14 .373 1.70 .455 2.26 .488 2.82 .498 0.01 0.12 .59 .222 1.15 .375 1.71 .456 2.27 .488 2.82 .498 0.04 .016 .00 .266 .116 .377 1.71 .456 2.27 .488 2.84 .498 0.05 .020 .61 .229 .117 .379 1.73 .458 2.29 .489 2.84 .498 0.05 .020 .61 .229 .117 .379 1.73 .458 2.29 .489 2.84 .498 0.06 .024 .62 .232 .118 .311 .174 .459 2.20 .489 2.84 .498 0.06 .024 .63 .232 .100 .331 .175 .460 2.31 .490 2.87 .498 0.80 .032 .64 </td <td>0.02 0.08 5.8 2.19 1.14 3.73 1.70 .455 2.26 .488 2.82 .498 0.03 0.12 .59 .222 1.15 .375 1.71 .456 2.27 .488 2.82 .498 0.04 0.16 .00 .222 1.15 .375 1.71 .456 2.27 .488 2.83 .498 0.05 .020 .61 .229 .117 .377 1.72 .457 2.28 .489 .2.84 .498 0.05 .020 .61 .229 .117 .379 1.73 .458 .2.29 .489 .2.84 .498 0.05 .024 .62 .232 .118 .174 .459 .2.30 .489 .2.86 .498 0.7 .028 .63 .236 .1.19 .383 .1.75 .460 .231 .490 .2.87 .498 0.80 .05 .424 <td< td=""><td>.000. 000.</td><td>.56 .212</td><td>1.12 .369</td><td>1.68 .454</td><td>2.24 .488</td><td>2.80 .497</td></td<></td>	0.02 0.08 5.8 2.19 1.14 3.73 1.70 .455 2.26 .488 2.82 .498 0.03 0.12 .59 .222 1.15 .375 1.71 .456 2.27 .488 2.82 .498 0.04 0.16 .00 .222 1.15 .375 1.71 .456 2.27 .488 2.83 .498 0.05 .020 .61 .229 .117 .377 1.72 .457 2.28 .489 .2.84 .498 0.05 .020 .61 .229 .117 .379 1.73 .458 .2.29 .489 .2.84 .498 0.05 .024 .62 .232 .118 .174 .459 .2.30 .489 .2.86 .498 0.7 .028 .63 .236 .1.19 .383 .1.75 .460 .231 .490 .2.87 .498 0.80 .05 .424 <td< td=""><td>.000. 000.</td><td>.56 .212</td><td>1.12 .369</td><td>1.68 .454</td><td>2.24 .488</td><td>2.80 .497</td></td<>	.000. 000.	.56 .212	1.12 .369	1.68 .454	2.24 .488	2.80 .497	
03 0.12 5.5 2.22 1.15 3.75 1.71 4.56 2.27 4.88 2.83 4.98 0.4 .016 .60 .226 1.16 .377 1.72 .457 2.28 .489 2.84 .498 0.5 .020 .61 .229 .117 .377 .173 .458 2.29 .489 2.85 .498 0.6 .024 .62 .322 .118 .811 .174 .459 2.30 .489 2.86 .498 0.6 .024 .62 .322 .119 .831 .174 .459 2.30 .489 2.86 .498 0.7 .028 .63 .366 .119 .831 .175 .460 2.31 .400 .287 .498 0.7 .028 .64 .231 .400 .287 .498 0.8 .032 .64 .231 .400 .284 .498	0.3 0.12 .59 .222 1.15 .375 1.71 .456 2.27 .488 2.83 .498 0.4 .016 .60 .226 1.16 .377 1.72 .457 2.28 .489 2.84 .498 0.5 .020 .61 .29 1.17 .379 1.73 .458 2.28 .489 2.84 .498 0.6 .024 .62 .232 1.17 .379 1.73 .458 2.29 .489 2.85 .498 .06 .024 .62 .232 1.18 .811 1.74 .459 2.30 .489 2.86 .498 .07 .028 .63 .326 1.120 .383 1.75 .400 2.31 .400 2.87 .498 .08 .032 .64 .230 .120 .385 1.76 .616 .232 .400 2.88 .498 .08 .055 .424	.01 .004	.57 .216	1.13 .371	1.69 .455	2.25 .488	2.81 .498	
04 .016 .60 .226 1.16 .377 1.72 .457 2.28 .489 2.84 .498 0.5 .020 .61 .229 .1.17 .379 1.73 .458 2.29 .489 2.84 .498 0.6 .024 .62 .221 .1.18 .381 1.74 .459 2.30 .489 2.86 .498 0.7 .028 .63 .236 1.19 .383 1.75 .460 2.31 .490 2.86 .498 0.8 .022 .64 .239 1.20 .385 1.75 .460 2.31 .490 2.86 .498 0.9 .036 .65 .242 1.21 .385 1.76 .461 2.32 .400 2.88 .498 .10 .040 .66 .245 1.21 .387 1.77 .462 2.33 .400 2.89 .498	0.4 0.16 .60 .226 1.16 .377 1.72 .457 2.28 .489 2.84 .498 0.5 .020 .61 .229 .1.17 .379 1.73 .458 .229 .489 .2.85 .498 0.6 .024 .62 .232 .1.18 .318 1.74 .459 .230 .489 .2.86 .498 0.7 .028 .63 .326 .1.19 .383 1.75 .460 .2.31 .490 .2.87 .498 .08 .032 .64 .230 .1.19 .383 1.75 .460 2.31 .490 .2.87 .498 .08 .032 .64 .230 .120 .385 1.76 .461 .2.32 .490 .2.88 .498 .08 .035 .464 .231 .172 .462 .2.31 .490 .2.88 .498 .09 .056 .424 .1.21 <t< td=""><td>.02 .008</td><td>.58 .219</td><td>1.14 .373</td><td>1.70 .455</td><td>2.26 .488</td><td>2.82 .498</td></t<>	.02 .008	.58 .219	1.14 .373	1.70 .455	2.26 .488	2.82 .498	
05 .020 .61 .229 .1.17 .379 1.7.3 .458 2.29 .489 2.85 .498 0.6 .024 .62 .323 .1.18 .81 .1.74 .459 .2.03 .489 2.85 .498 0.6 .024 .62 .323 .1.18 .81 .174 .459 .2.03 .489 2.85 .498 0.7 .028 .63 .236 .119 .838 .175 .400 2.31 .490 2.87 .498 .08 .032 .64 .239 .120 .385 .176 .401 2.32 .490 2.88 .498 .09 .036 .65 .242 .121 .387 .177 .462 2.33 .490 2.89 .498 .09 .06 .245 .1.22 .389 .178 .463 .244 .490 .290 .498	0.5 0.20 6.61 2.29 1.17 3.79 1.73 4.58 2.29 4.89 2.85 4.98 0.6 .024 .62 .323 1.18 .381 1.74 .459 2.30 .489 2.86 .498 0.7 .028 .63 .230 1.19 .381 1.74 .459 2.30 .489 2.87 .498 0.8 .022 .64 .230 1.20 .385 1.76 .461 2.32 .498 .498 0.9 .036 .65 .424 1.21 .387 1.77 .461 2.31 .490 2.88 .498	.03 .012	.59 .222	1.15 .375	1.71 .456	2.27 .488	2.83 .498	
06 0.24 6.2 2.32 1.18 .81 1.74 .459 2.30 .489 2.86 .498 0.7 .028 .63 .236 1.19 .383 1.75 .460 2.31 .490 2.87 .498 0.8 .032 .64 .239 1.20 .385 1.76 .61 2.32 .490 2.88 .498 0.9 .036 .65 .242 1.21 .387 1.77 .462 2.33 .490 2.88 .498 .10 .040 .66 .245 1.22 .387 1.77 .462 2.33 .490 2.89 .498	06 0.24 6.2 2.32 1.18 .881 1.74 .459 2.30 .489 2.86 .498 0.7 .028 .63 .236 1.19 .383 1.75 .460 2.31 .490 2.87 .498 0.8 .032 .64 .239 1.20 .385 1.76 .616 2.32 .400 2.88 .498 0.8 .032 .65 .242 1.21 .387 1.77 .462 2.33 .490 2.88 .498	.04 .016	.60 .226	1.16 .377	1.72 .457	2.28 .489	2.84 .498	
07 .028 .63 .236 1.19 .383 1.75 .460 2.31 .490 2.87 .498 08 .032 .64 .239 1.20 .385 1.76 .461 2.32 .490 2.88 .498 09 .036 .65 .242 .121 .387 .177 .462 2.33 .400 2.88 .498 .10 .040 .66 .245 .121 .387 .177 .462 2.33 .400 2.89 .498 .10 .040 .66 .425 .122 .389 .178 .463 .2.34 .490 2.90 .498	0.07 .028 .6.3 .2.36 .1.19 .383 1.75 .4.60 .2.31 .4.90 .2.87 .4.98 <th .4.9<="" td=""><td>.05 .020</td><td>.61 .229</td><td>1.17 .379</td><td>1.73 .458</td><td>2.29 .489</td><td>2.85 .498</td></th>	<td>.05 .020</td> <td>.61 .229</td> <td>1.17 .379</td> <td>1.73 .458</td> <td>2.29 .489</td> <td>2.85 .498</td>	.05 .020	.61 .229	1.17 .379	1.73 .458	2.29 .489	2.85 .498
08 0.32 .64 .239 1.20 .385 1.76 .461 2.32 .490 2.88 .498 0.9 .036 .65 .242 1.21 .387 1.77 .462 2.33 .490 2.89 .498 .10 .040 .66 .245 1.22 .389 1.78 .463 2.34 .490 2.90 .498	.08 .032 .64 .239 1.20 .385 1.76 .461 2.32 .490 2.88 .498 .09 .036 .65 .242 1.21 .387 1.77 .462 2.33 .490 2.89 .498	.06 .024	.62 .232	1.18 .381	1.74 .459	2.30 .489	2.86 .498	
.09 .036 .65 .242 1.21 .387 1.77 .462 2.33 .490 2.89 .498 .10 .040 .66 .245 1.22 .389 1.78 .463 2.34 .490 2.90 .498	.09 .036 .65 .242 1.21 .387 1.77 .462 2.33 .490 2.89 .498	.07 .028	.63 .236	1.19 .383	1.75 .460	2.31 .490	2.87 .498	
.10 .040 .66 .245 1.22 .389 1.78 .463 2.34 .490 2.90 .498		.08 .032	.64 .239	1.20 .385	1.76 .461	2.32 .490	2.88 .498	
	.10 .040 .66 .245 1.22 .389 1.78 .463 2.34 .490 2.90 .498	.09 .036	.65 .242	1.21 .387	1.77 .462	2.33 .490	2.89 .498	
51		.10 .040	.66 .245	1.22 .389	1.78 .463	2.34 .490	2.90 .498	
	51					51		

